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L_2 -Boosting algorithm applied to high-dimensional problems in genomic selection

OSCAR GONZÁLEZ-RECIO^{1*}, KENT A. WEIGEL², DANIEL GIANOLA^{2, 3, 4},
HUGO NAYA⁵ AND GUILHERME J. M. ROSA²

¹ Departamento de Mejora Genética Animal, Instituto Nacional de Investigaciones Agrarias, Madrid 28040, Spain

² Department of Dairy Science, University of Wisconsin, Madison, WI 53706, USA

³ Department of Animal Sciences, University of Wisconsin, Madison, WI 53706, USA

⁴ Department of Animal and Aquacultural Sciences, Norwegian University of Life Sciences, P.O. Box 5003, N-1432, Ås, Norway

⁵ Unidad de Bioinformática, Instituto Pasteur de Montevideo, Montevideo 11400, Uruguay

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Summary

The L_2 -Boosting algorithm is one of the most promising machine-learning techniques that has appeared in recent decades. It may be applied to high-dimensional problems such as whole-genome studies, and it is relatively simple from a computational point of view. In this study, we used this algorithm in a genomic selection context to make predictions of yet to be observed outcomes. Two data sets were used: (1) productive lifetime predicted transmitting abilities from 4702 Holstein sires genotyped for 32 611 single nucleotide polymorphisms (SNPs) derived from the Illumina[®] BovineSNP50 BeadChip, and (2) progeny averages of food conversion rate, pre-corrected by environmental and mate effects, in 394 broilers genotyped for 3481 SNPs. Each of these data sets was split into training and testing sets, the latter comprising dairy or broiler sires whose ancestors were in the training set. Two weak learners, ordinary least squares (OLS) and non-parametric (NP) regression were used for the L_2 -Boosting algorithm, to provide a stringent evaluation of the procedure. This algorithm was compared with BL [Bayesian LASSO (least absolute shrinkage and selection operator)] and BayesA regression. Learning tasks were carried out in the training set, whereas validation of the models was performed in the testing set. Pearson correlations between predicted and observed responses in the dairy cattle (broiler) data set were 0.65 (0.33), 0.53 (0.37), 0.66 (0.26) and 0.63 (0.27) for OLS-Boosting, NP-Boosting, BL and BayesA, respectively. The smallest bias and mean-squared errors (MSEs) were obtained with OLS-Boosting in both the dairy cattle (0.08 and 1.08, respectively) and broiler (−0.011 and 0.006) data sets, respectively. In the dairy cattle data set, the BL was more accurate (bias = 0.10 and MSE = 1.10) than BayesA (bias = 1.26 and MSE = 2.81), whereas no differences between these two methods were found in the broiler data set. L_2 -Boosting with a suitable learner was found to be a competitive alternative for genomic selection applications, providing high accuracy and low bias in genomic-assisted evaluations with a relatively short computational time.

1. Introduction

Considerable effort is being made to develop and improve statistical models that increase cross-validation accuracy in genome-wide association studies or

genome-assisted prediction of phenotypes. Bayesian methods, which use shrinkage to estimate regressions of phenotypes on single nucleotide polymorphism (SNP) genotypes, have gained attention for this purpose. However, some of the Bayesian specifications proposed have statistical drawbacks, such as strong assumptions on the prior distribution of marker variance, or difficulties in capturing complex SNP signals (Gianola *et al.*, 2009). Besides, these methods

* Corresponding author. Departamento Mejora Genética Animal, Instituto Nacional de Investigación y Tecnología Agraria y Alimentaria, Madrid 28040, Spain. Tel: +34913471486, e-mail: gonzalez.oscar@inia.es

may lose accuracy when markers are sparse, e.g. with low-density genotyping or when pre-selection of SNPs is practiced (Solberg *et al.*, 2008; Weigel *et al.*, 2009). This may be important when predicting genomic breeding values in populations in which large-scale genotyping is available (e.g. cattle and poultry), or for tagging SNPs in diagnosis of genetic diseases (Lowe *et al.*, 2004). Non-parametric (NP) methods seem to be less influenced by marker density (Gianola *et al.*, 2006; Gonzalez-Recio *et al.*, 2008, 2009). However, this class of methods has not yet gained as much attention as Bayesian linear regression methods, probably because their interpretation is less straightforward and, depending on the implementation, may be computationally more complex.

The use of methods that involve some sort of variable selection is pertinent in problems with a large number of predictor variables, such as genomic selection. Machine-learning algorithms have been introduced in a genomic selection context (Long *et al.*, 2007), and these may be useful for increasing the accuracy of predictions using pre-selected SNPs in prediction models (Szymczak *et al.*, 2009). Boosting is a procedure that has not yet been studied in a genomic selection context. It is a machine-learning ensemble method, which means that several models are somehow combined to improve the predictive ability. The manner in which models are combined, labels the ensemble method (e.g. model averaging, bagging or boosting). The original *AdaBoost* algorithm (Freund & Schapire, 1996) and modifications thereof have attracted much attention in several fields of science, due to their good empirical performance. These algorithms have been shown to be powerful in classification problems (Opitz & Maclin, 1999). One of the most interesting modifications is the L_2 -Boosting algorithm for regression in high-dimensional problems, which also has advantages when a non-null covariance structure between explanatory covariates exists, e.g. SNPs in high linkage disequilibrium. This version of boosting considers an L_2 loss function in a recursive fashion, and its statistical properties and performance have been described by several authors (e.g. Bühlmann, 2006; Lutz *et al.*, 2008).

The objectives of this study were: (1) to apply L_2 -Boosting with two different weak learners in two different genome-assisted genetic evaluation scenarios and (2) to compare L_2 -Boosting with BayesA and BL [Bayesian LASSO (least absolute shrinkage and selection operator)] models, which are methods commonly used to compute genome-assisted evaluations. This provides a strong test of the hypothesis of whether or not L_2 -Boosting with weak learners can attain the predictive ability of complex Bayesian hierarchical models.

2. Material and methods

(i) Data

Two data sets from different species (dairy cattle and broilers) were analysed. These data sets are briefly described next.

(a) Dairy cattle

High-density SNP genotypes of 4702 Holstein sires, which were derived from the Illumina[®] BovineSNP50 BeadChip, and their respective progeny test predicted transmitting abilities (PTAs) for the length of productive life (PL), were obtained from the Bovine Functional Genomics Laboratory and Animal Improvement Programs Laboratory, respectively, at the USDA-ARS Beltsville Agricultural Research Center (Beltsville, MD). The aforementioned PTAs were computed using a genetic evaluation model that assumes the existence of an infinite number of loci, each with an infinitesimally small additive effect. Genotypes at each SNP locus were coded arbitrarily as 0 (homozygous for allele *B*), 1 (heterozygous), 2 (homozygous for allele *b*) or 5 (missing). The 38 416 SNPs used in the study of VanRaden *et al.* (2009) were edited further. Monomorphic SNPs, SNPs with minor allele frequency (MAF) <0.05, and SNPs with >10% missing genotypes were excluded from the analyses. Information from flanking markers was used to impute the most probable genotypes for other loci with missing genotypes, based on the conditional probability of observing a particular configuration at a locus in question given genotypes at both neighbouring markers. This led to a total of 32 611 SNPs for the analyses described herein. The data were split such that a training data set contained ancestors and contemporary individuals, and a testing set represented the progeny of these individuals whose phenotypes (PTAs) were regarded as yet to be observed. The training set included PL PTAs (standardized to attain a distribution with a null mean and variance equal to 1) from the 2003 routine genetic evaluation of 3304 sires born before 1998. The testing set included the standardized PL PTAs from the 2008 routine genetic evaluation of 1398 sires born after 1998. Further details on this data set are in Weigel *et al.* (2009).

(b) Broilers

The data consisted of average food conversion rate (FCR) records of the progeny of 394 sires from a commercial broiler line in the breeding program of Aviagen Ltd (Newbridge, Scotland, UK). Prior to the analyses, the individual bird FCR records were adjusted for environmental and mate of sire effects. Genotypes consisted of 4505 SNPs distributed along

the genome. All SNPs with monomorphic genotypes or with MAF < 5% were excluded. After editing, genotypes consisted of 3481 SNPs. The data set was also split into training and testing sets. Sires included in the testing set were required to have more than 20 progeny with FCR records to ensure a reliable mean phenotype, and they were required to have sires in the training set. Sixty-one sires (15.5% of the total) were included in the testing set, whereas the remaining 333 sires were in the training set. Predictions were calculated from the training set, and the accuracy of predicting the mean progeny phenotype was assessed using sons in the testing set. More details on this data set can be found in Gonzalez-Recio *et al.* (2009).

In the two data sets, the same families could be represented in both training and testing sets, so the procedures utilize both linkage disequilibrium and linkage information. Clustering different families within either training or testing sets is difficult when using livestock data, because families and generations usually overlap. From a genomic selection point of view, the approach utilized herein is realistic, because the typical objective is to determine which sires are to be chosen from the current population for use as parents of the next generation.

(ii) L₂-Boosting for high-density genotypes

This learning technique is based on the *AdaBoost* algorithm described by Freund & Schapire (1996), and it combines several weak learners to form a ‘committee’ with potentially greater predictive ability than that of any of the individual learners. A weak learner is defined as a predictive method with a slightly better performance than random guessing. Although boosting was originally designed for classification problems, it was extended to regression by Friedman (2001). Bühlmann & Yu (2003) proposed a version of boosting with the L₂ loss function for regression and classification, which is called L₂-Boosting. The L₂ loss function measures the degree of wrongness of the predictions using a quadratic term with the form $L_2 \text{ loss} = f(y - \hat{y}) = (y - \hat{y})^2$. The authors also showed that L₂-Boosting may be used for regression in high-dimensional problems by doing some type of covariate selection through a small-step gradient descent. The L₂-Boosting algorithm for regression problems involving s genomic markers (with s being very large and possibly $s \gg n$, where n is the training sample size) is described next.

Consider the model

$$\mathbf{y} = g(\mathbf{x}_p) + \mathbf{e},$$

where \mathbf{y} is an $n \times 1$ vector of records; \mathbf{x}_p is a vector of genotype codes of n individuals for the SNP locus p ; $g(\mathbf{x}_p)$ is an unknown function to be learned and interpretable as $E(\mathbf{y}|\mathbf{x}_p)$ and \mathbf{e} is a vector of residuals

assumed to be identically and independently distributed, and also independent of \mathbf{x}_p . Different learners may be used to learn about $g(\mathbf{x}_p)$. Here, two different learners (linear and non-linear) were employed. The linear learner was ordinary least squares (OLS; OLS-BOOST) regression, and the non-linear learner was NP (NP-BOOST) regression. *A priori*, NP would be expected to capture both additive and non-additive signals. Once the learners have been set, the boosting algorithm works as follows:

Step 1 (Initialization): Given the data (y, x) , apply the weak learner procedure to each SNP one at a time, yielding the function estimate $f_0(\cdot) = \hat{g}(\mathbf{x}_p)$, where $\hat{g}(\mathbf{x}_p)$ is estimated from the original data set, with $p = \arg \min_p \sum_{i=1}^n (y_i - \hat{g}(x_{i,p}))^2$. Set $m = 1$. Let the prediction of phenotypes be $\hat{y} = f_0(\cdot)$.

Step 2. Compute residuals as $\mathbf{r}_m = \mathbf{y} - \sum_{i=0}^{m-1} v_i f_i(\cdot)$, and fit the weak learner for each SNP p ($p \in 1, \dots, s$) to current residuals, where v is a shrinkage parameter describing the step size when updating the residuals. Without loss of generality, v can be assumed as constant and small ($0 < v < 1$), but it may be optimized to balance the predictive ability and computation time. Select SNP p , where $p = \arg \min_p \sum_{i=1}^n (r_i - \hat{g}(x_{i,p}))^2$ and set $f_m(\cdot) = \hat{g}(\mathbf{x}_p)$. Here, v equal to 0.1 and 0.01 was used for OLS-BOOST and NP-BOOST, respectively.

Step 3. Update predictions as $\hat{y}_m^i = \hat{y}_{m-1}^i + v f_m(r_i, x_{i,p})$, ($i \in \{1, \dots, n\}$), where $f_m(r_i, x_{i,p})$ is the estimate for individual i obtained by regressing the current residual (r_i) at iteration m on its genotype for SNP p ($x_{i,p}$).

Step 4. Increase the iteration index m by 1, and repeat steps 2–4 until a convergence criterion is reached.

As stated, the two weak learners used were OLS-BOOST and NP-BOOST. The NP learner is less commonly known and a description is given in Appendix A. Boosting yields an additive model whose terms are fitted in a stepwise fashion. Note that the function $g(\mathbf{x}_p)$ does not assume linearity when using NP-BOOST.

Boosting algorithms for regression have been interpreted as functional gradient descent techniques (Bühlmann, 2006), and L₂-Boosting may be viewed as a sequence of Hilbert spaces in what is known as a ‘weak greedy algorithm’. Boosting is one of the most successful and practical methods in the machine-learning field. It has great flexibility and can capture complexity introduced by covariates, such as SNPs. Although it was first thought as a black box, its statistical properties have been described by some authors (Bühlmann, 2006; Cornillon *et al.*, 2008).

(iii) Convergence criterion

This can be viewed as a model selection problem, and stopping rules based on criteria such as the Bayesian Information Criterion (BIC), Akaike Information

Criterion (AIC), a corrected version of AIC (AIC_c), or generalized cross validation (GCV) can be used. Other criteria have been proposed, but there is some consensus on the benefits of GCV (Bühlmann, 2006; Cornillon *et al.*, 2008; Lutz *et al.*, 2008). In this study, a 10-fold cross validation was utilized to tune the optimal number of iterations, as follows. Ten per cent of the observations, which were randomly sampled from the training set, were kept as the tuning set. Steps 1, 2 and 3 of the boosting algorithm were performed on the training set, without including observations of the tuning set. The convergence criterion (Step 4) was determined as follows. Mean-squared error (MSE) was computed in the tuning set at each iteration as

$$\text{MSE}_{\text{tune}} = t^{-1} \sum_{j=1}^t (y_j - \hat{y}_j)^2,$$

where t is the number of individuals in the tuning set, y_j is the observed response of individual j in the tuning set and \hat{y}_j is its predicted response calculated at each iteration after selecting the SNPs that minimized MSE in the training set. The optimal number of iterations was that which minimized MSE in the tuning set, after running a large enough number of iterations. Note that the training set was used to make the inferences, and the tuning set to determine the iteration at which the algorithm would be stopped.

Predictions in the testing set were computed at the optimal iteration. Since a 10-fold GCV was used, 10 independent tuning sets were created in 10 different analyses, and predictions in the testing set were averaged across runs. Note that this GCV scheme creates independence between the testing and tuning sets. The maximum number of boosting iterations was set to 5000. An illustration of the algorithm framework is given in Fig. 1.

These two boosting algorithms were compared with BayesA and BL, two methods that have received attention in genomic selection (Meuwissen *et al.*, 2001; de los Campos *et al.*, 2009; Weigel *et al.*, 2009). Details on BayesA and BL are given in Appendices B and C, respectively. For these methods, a tuning set is not necessary and the whole training set was used for inferences.

There is some similarity between L_2 -Boosting and LASSO. However, these methods differ as shown by Bühlmann (2006), and a different variance-bias trade-off is achieved by each approach. They also differ in the maximum number of predictor variables allowed in the model. The maximum number of covariates selected by the original LASSO, as proposed by Tibshirani (1996), is $\min(n, s + 1)$ including an intercept, where s is the number of covariates. In the Bayesian counterpart of LASSO (Park & Casella, 2008), all estimates of regressions on markers are shrunk towards zero (but never set to exactly zero)

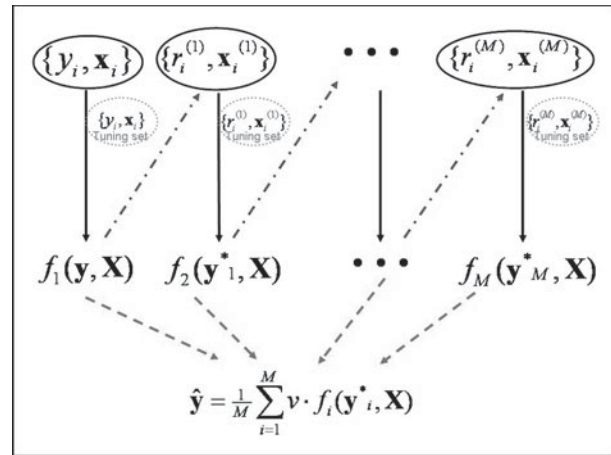


Fig. 1. Schematic diagram of the boosting framework. Each weak learner $f_m(y, X)$ is trained on a weighted form of the training set (→), which are the residuals from the previous weak learner (---). The weak learner is tested on a tuning set at each iteration. Once all weak learners have been trained, those from iteration 1 to that minimizing MSE in the tuning set are combined to provide final estimates \hat{y} (---). Adapted from Bishop (2006).

using a conditional Laplace prior assigned to regression coefficients. In this case, the maximum number of influential covariates is s , and an ad-hoc threshold must be used to set the number of desired covariates, if so desired. On the other hand, the number of covariates selected in L_2 -Boosting depends on the number of iterations until the chosen convergence criterion is reached, and a particular covariate could be selected several times or might not be selected at all.

(iv) Validation criteria

Correlations between true and predicted phenotypes and MSE for each method were calculated. Larger correlations and smaller MSE values indicate better performance of the model. Bias was calculated as $s^{-1} \sum_{i=1}^s (y_i - \hat{y}_i)$, where s is the number of individuals in the testing set. *A priori*, a method with smaller bias is preferable unless its variance is too large.

Realized observations in the testing set (y_{test}) were regressed on their predictions (\hat{y}_{test}) as

$$y_{\text{test}} = a + b \cdot \hat{y}_{\text{test}} + \varepsilon,$$

where a is the intercept, b is a regression coefficient and ε is a residual. An unbiased method is expected to have $a=0$ and $b=1$. Values of the slope that are above or below one would indicate under-prediction or over-prediction, respectively.

3. Results and discussion

The estimated shrinkage parameter λ of BL was 205.9 for the dairy cattle data set and 69.5 for the broiler

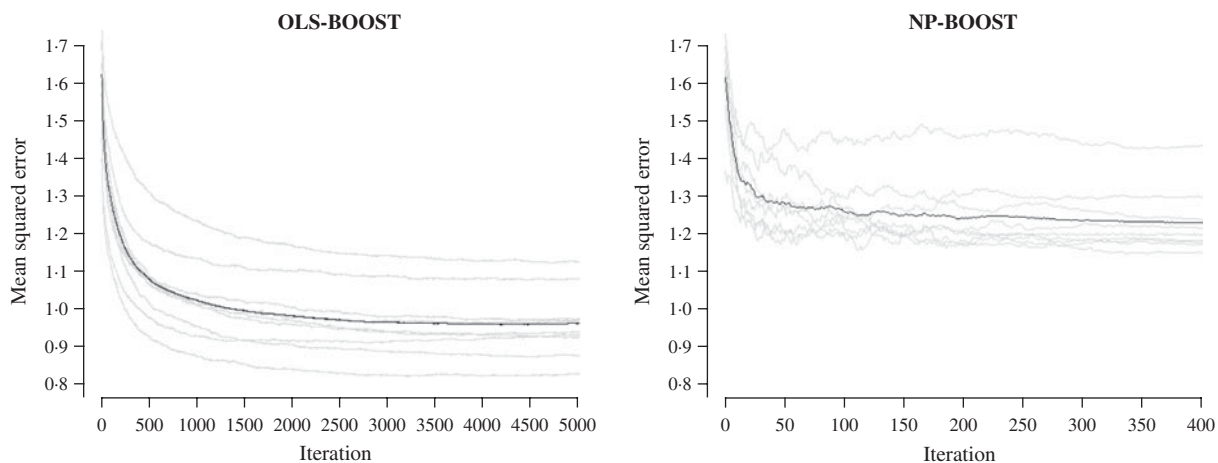


Fig. 2. MSE at each iteration for OLS-BOOST and NP-BOOST in the dairy cattle tuning set in each of the 10 folds (grey line) and the averaged MSE across folds (black solid line).

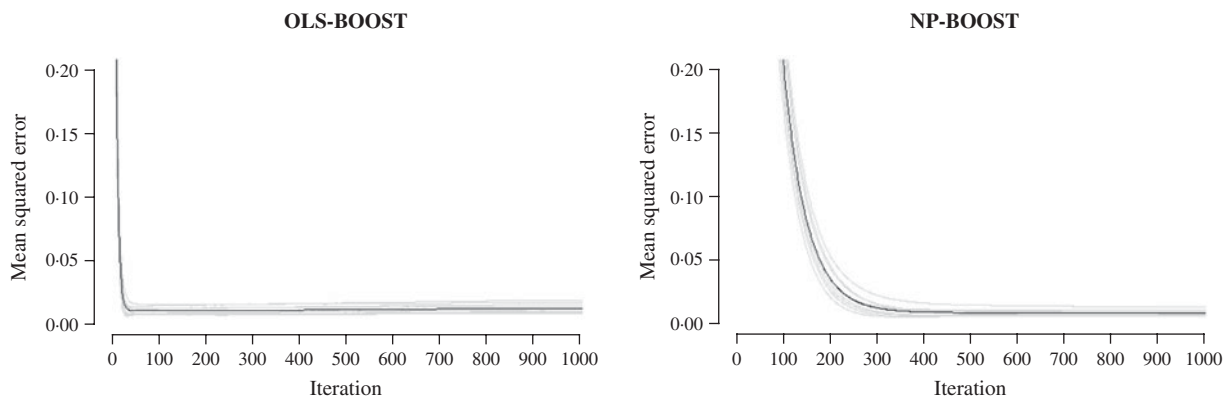


Fig. 3. MSE at each iteration for OLS-BOOST and NP-BOOST in the broiler tuning set in each of the 10 folds (grey line) and the averaged MSE across folds (black solid line). For convenience, only the first 1000 iterations are shown.

data set, with posterior standard deviations equal to 2.4 and 2.2, respectively. These estimates suggest greater shrinkage in the dairy data, which was expected due to the larger number of markers in this data set. The average time per iteration (calculated in the same workstation) in the dairy cattle data set was 12.4 s for BayesA, 12.1 s for BL, 3.4 s for OLS-BOOST and 4.1 h for NP-BOOST; whereas 0.04 s were needed for BayesA, BL and OLS-BOOST and 16.66 s for NP-BOOST in the broiler data set. Note also that the number of iterations needed was lower for the boosting algorithms. OLS-BOOST required less computer time than the other methods, which may be an advantage when using large data sets with several thousands or millions of markers. The NP-BOOST algorithm seemed to be too time-consuming in large data sets. Nonetheless, the time per iteration is dependent on hardware and software used.

Figures 2 and 3 show the MSE obtained for each fold of GCV in the tuning set at each iteration of OLS-BOOST and NP-BOOST in the cattle and poultry data sets, respectively. These plots allow the

visual inspection of convergence of the boosting algorithm. With a smaller step size (ν), the algorithm converged more slowly. OLS-BOOST (MSE=0.96) had better performance than NP-BOOST (MSE=1.23) in the dairy cattle tuning set. It must be pointed out though that NP-BOOST was not optimized in this data set, because the computation time per iteration was prohibitive. Because of slow convergence, the step size $\nu=0.01$ in NP-BOOST was increased to $\nu=1$, resulting in under-performance of this weak learner. It is essential to monitor the tuning set, because L_2 -Boosting often yields the fully saturated model, which fits the training data perfectly, and the bias and prediction variance explode as iteration proceeds (Bühlmann & Yu, 2003). Initial iterations of the algorithm are expected to have a large bias and a low prediction variance. As the model becomes more complex, with a larger number of SNPs having a non-zero effect, the algorithm uses the training set more effectively and is able to adapt to more complicated underlying genetic systems. This may lead to lower bias but higher variance, which suggests over-fitting in

Table 1. Pearson correlation between yet to be observed records and their predictions in each testing set for L_2 -Boosting with OLS regression or NP regression as weak learners, BayesA and BL

Method	Dairy cattle	Broilers
OLS-BOOST	0.65	0.33
NP-BOOST	0.53 ¹	0.37
BayesA	0.63	0.27 ²
BL	0.66	0.26

¹ Results not optimized due to large computation time per iteration.

² Results from Gonzalez-Recio *et al.* (2009).

the training set. Hence, the algorithm must be stopped at an iteration that provides intermediate complexity for the prediction of future records.

Pearson correlations of predictions obtained with each method in the testing sets are shown in Table 1. Pearson correlations between predicted and observed phenotypes were similar for all methods in the dairy cattle data set, ranging between 0.63 and 0.66, except for NP-BOOST, which yielded a Pearson correlation of 0.53 without optimizing the algorithm, due to the computation time, as stated above. These correlations were similar to those obtained by VanRaden *et al.* (2009), who regressed daughter yield deviations for PL on 40 426 SNPs in a sample from the same Holstein population using a linear Bayesian regression model with an adjustment for the reliability of parent average. In the broiler data, L_2 -Boosting produced larger Pearson correlations (OLS-BOOST = 0.33 and NP-BOOST = 0.37) than those obtained with Bayesian regressions (0.26–0.27). The L_2 -Boosting algorithm with NP as a weak learner had up to 42% greater accuracy than the linear Bayesian regression models using progeny means as response variables in the broiler data set. In this data set, the NP weak learner outperformed OLS in prediction accuracy, suggesting that it may capture more genetic (additive and non-additive) variance from the data.

The Pearson correlation obtained with L_2 -Boosting was larger than those obtained by Gonzalez-Recio *et al.* (2009) and Long *et al.* (2010) using different models on the same data set. However, confidence intervals presented by Gonzalez-Recio *et al.* (2009) overlapped with those obtained in this study, and Long *et al.* (2010) found a slightly smaller MSE using radial basis functions.

Bias and MSE of predictions from each method are shown in Table 2. The OLS-BOOST algorithm had the smallest MSE (1.08) in the dairy cattle testing set followed by BL (1.10), and in the broiler data set (0.006) followed by NP-BOOST (also 0.006). BayesA had the poorest MSE (2.81) in the dairy cattle data

Table 2. Bias and MSE of predicted responses in each testing set for L_2 -Boosting with OLS regression or NP regression as weak learners, BayesA and BL

Method	Dairy cattle		Broilers	
	Bias	MSE	Bias	MSE
OLS-BOOST	0.08	1.08	−0.011	0.006
NP-BOOST	0.57 ¹	1.67 ¹	−0.018	0.006
BayesA	1.26	2.81	−0.016 ²	0.007 ²
BL	0.10	1.10	−0.010	0.007

¹ Results not optimized due to large computing time per iteration.

² Results from Gonzalez-Recio *et al.* (2009).

set, and this was almost 2.6 times greater than the MSE obtained with OLS-BOOST. However, in the broiler data set, MSE was similar for all four methods, with a slight advantage for boosting. OLS-BOOST and BL produced the smallest bias in both dairy cattle (0.08 and 0.10, respectively) and broiler (−0.011 and −0.010, respectively) data. BayesA and NP-BOOST had the largest bias in the dairy cattle (1.26, 0.57) and broiler (−0.016, −0.018) data sets. Differences in bias between OLS-BOOST and BL in the dairy cattle data set have to be taken cautiously, as phenotype distributions in the training and testing data sets were normalized and centred, ignoring the genetic trend that, although small, may exist.

The Bayesian regression methods estimated the slope of the regression of observed on predicted values at 0.71 and 1.34 in the dairy cattle data set (Fig. 4). Bayesian regression methods produced smaller slopes (0.36) in the broiler data set (Fig. 5). These results suggest better agreement between observed responses and their predictions obtained with L_2 -Boosting. The BL and BayesA tended to underestimate the true progeny means in the broiler data, whereas OLS-BOOST overestimated them.

Similar regression coefficients ranging between 0.71 and 0.86 have been found by other authors (VanRaden *et al.*, 2009; Aguilar *et al.*, 2010) for overall conformation, working with a similar population but using different versions of the so-called ‘genomic BLUP’ (VanRaden, 2008). Aguilar *et al.* (2010) obtained a regression of observed on predicted response of 0.86 using a single-step approach with phenotypes from several million animals. Results obtained with OLS-BOOST in this study were similar to those recently reported by the USDA for the same trait (the squared correlation was 0.31 and the slope of the regression was estimated at 1.08), but that study used a larger number of records and used daughter yield deviation as response variable, instead of the PTA values used here.

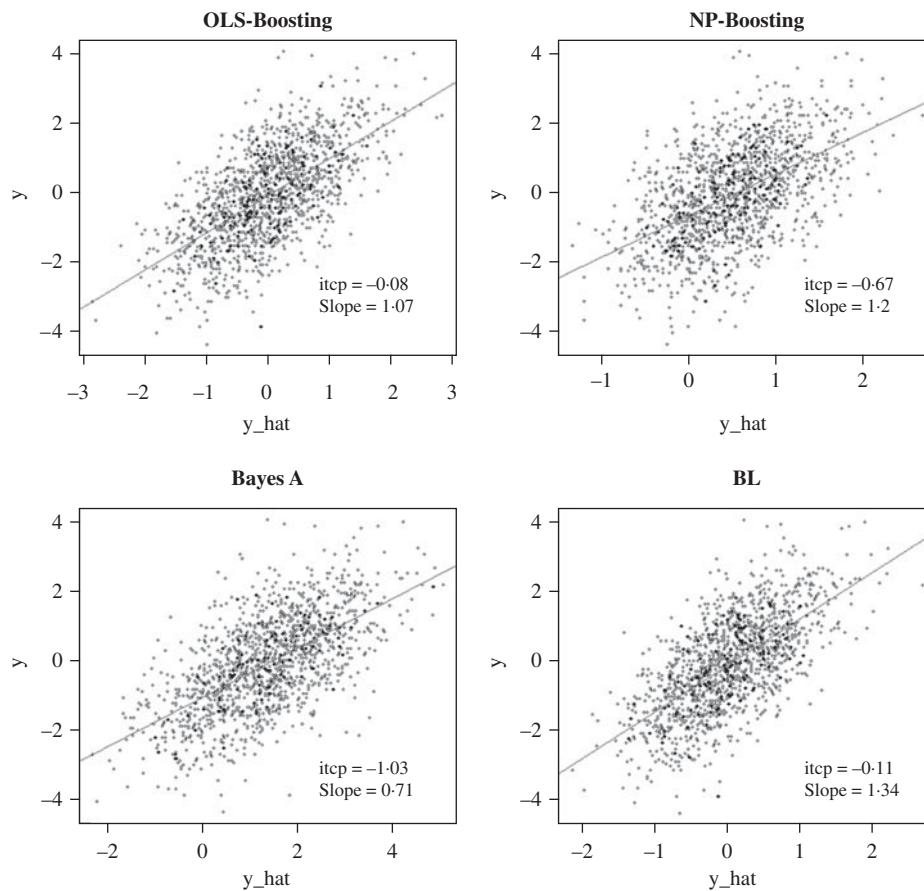


Fig. 4. Relationship between 2008 progeny test PTA for productive lifetime (y) and 2003 genomic PTA (y_{hat}) in a testing set comprised 1398 Holstein bulls born from 1999 to 2002 using L_2 -Boosting with OLS regression or NP regression as weak learners, and with BayesA and BL. Intercept and slope estimates from the linear regressions are given.

In summary, BL and OLS-BOOST had better predictive ability in the dairy cattle data set than BayesA and NP-BOOST. The two former methods provided greater accuracy (larger Pearson correlation and smaller MSE), with some advantages for OLS-BOOST in terms of bias. In the broiler data set, L_2 -Boosting provided the highest correlations and smallest MSE of prediction of yet-to-be observed phenotypes although NP-BOOST showed some bias. It must be pointed out that the need for a tuning set in the L_2 -Boosting algorithm may be a disadvantage relative to BL and BayesA, which use the whole training set for making inferences. The main difference between L_2 -Boosting and other methods commonly used, such as partial least squares, Bayesian regressions or reproducing kernel Hilbert spaces is that L_2 -Boosting is trained using a sequence of residuals from previous iterations in a weighted fashion. Only the covariate (SNP) that minimizes the loss function is used at each iteration, and a small step is taken towards modelling the real observations.

Differences between these data sets must be emphasized. The dairy cattle data set had a larger number of data points and SNPs, and its response variable

was PTAs predicted from a model that assumed additivity and normality, which is expected to reflect additive genetic effects only, instead of the average progeny performance. Also, as stated earlier, a PTA is a smoothed product from a predictive model which may hide signals that are actually present in the data, although it is expected to account for some part of epistatic variance acting in an additive manner (Hill *et al.*, 2008). It must be pointed out that PTA may also include a contribution from parents' information.

Several authors have shown that boosting may increase accuracy in regression analysis. For example, Friedman (2001) and Opitz & Maclin (1999) reported benefits of boosting using 23 different data sets, indicating that it can create ensembles that are often more accurate than those from other ensemble methods, such as bagging (Breiman, 1996). However, Opitz & Maclin (1999) also showed that the *Ada-Boosting* algorithm may be sensitive to noisy data and may be prone to over-fitting, although this was later questioned by Bühlmann & Yu (2006).

Results from our study suggest that performance of L_2 -Boosting may depend on the weak learner chosen

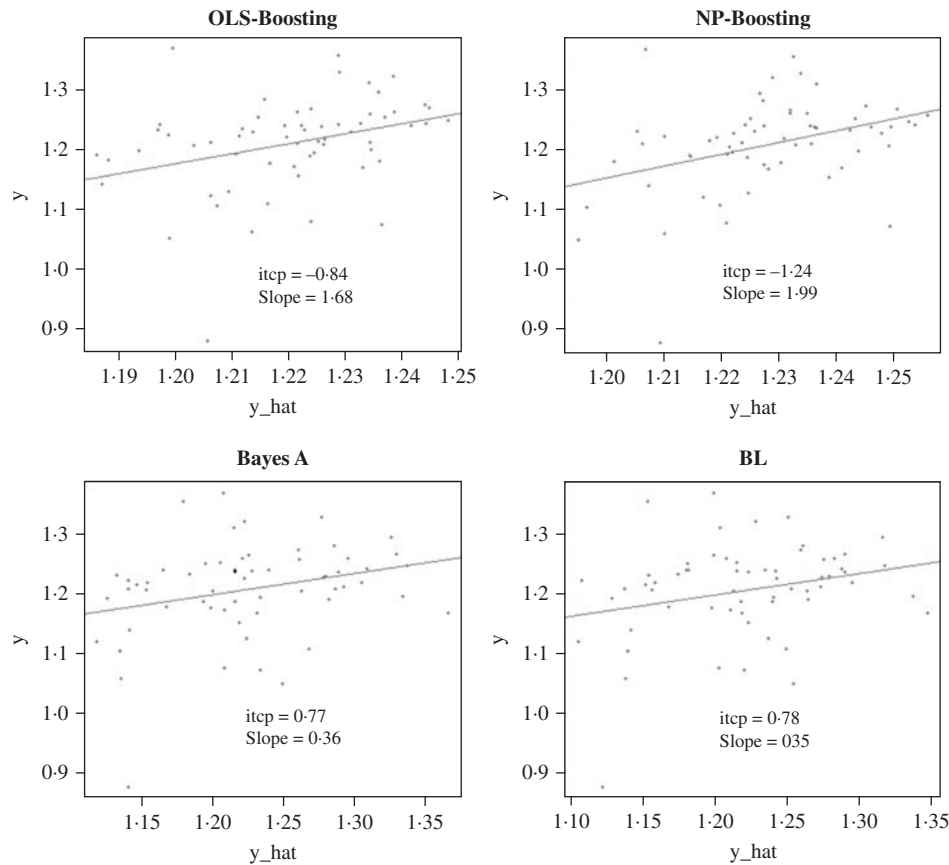


Fig. 5. Relationship between observed average FCR, adjusted by environmental and mate effects, (y) and the genomic predicted FCR (y_{hat}) in a testing set comprised 61 broilers, which were progeny of 394 broilers in the training set using L_2 -Boosting with OLS regression or NP regression as weak learners, and BayesA and BL. Intercept and slope estimates from the linear regressions are given.

and the step size used. We used two arbitrarily chosen weak learners from a large variety of candidates, and the performance of each may depend on the underlying problem (state of nature). Further, a small value of the step-size parameter (ν) should be used for convenience, but it can be optimized, if possible, when computing time is a limiting factor. Smaller values of ν increase the degree of weakness of a learner. Smaller values of ν were tested for both learners (results not shown), without improving accuracy, but with a corresponding increase in the computing time (except for NP-BOOST in the dairy cattle data set, as noted above).

The results obtained in this study should hold provided there is genetic or molecular similarity, whereas the absence thereof may yield different performance, but this must be evaluated on a case-by-case basis.

4. Conclusions

Our results highlight the potential ability of L_2 -Boosting of attaining high accuracy and small bias in high-dimensional problems, such as genomic selection, when a suitable weak learner is used. This makes

such algorithms appealing for selecting signal covariates in whole-genome studies. L_2 -Boosting seemed to be appealing for scenarios in which more noise exists. BL may yield similar accuracy as L_2 -Boosting under linear and additive scenarios. In a genomic selection context, a higher correlation between predicted and observed responses is desirable, and the boosting algorithm seemed competitive in this regard. Other methods commonly used in genomic-assisted evaluation yielded similar accuracy, as shown here and in recent scientific literature. However, unbiased and reliable predictions are necessary to compare animals or plants in commercial breeding programmes. Differences in MSE and bias may assist in determining which method is preferred for the prediction of individual total genomic merit of the traits of interest in a given species.

Overall, L_2 -Boosting seems to be a viable alternative to more widely used methods of the prediction of the total genomic merit of animals and plants that are candidates as parents of future generations. However, its promising behaviour must be studied further in a whole genomic evaluation context. Among other issues, the choice of weak learner, stopping criterion,

step-size parameter and programming strategy (such as parallelization) may be considered in future studies to improve the performance of the algorithm.

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Appendix A

A NP regression on genomic markers for animal breeding was proposed first by Gianola *et al.* (2006) and applied to chicken mortality by Gonzalez-Recio *et al.* (2008). Consider the model

$$\mathbf{y} = \mathbf{g}(\mathbf{x}_i) + \mathbf{e},$$

where $\mathbf{y} = y_i$ is the $(n \times 1)$ vector of responses and \mathbf{x}_i is a $(n \times 1)$ vector representing the genotype of individual i ($i \in \{1, \dots, n\}$) for p SNP loci. Here, $g(\mathbf{x}_i)$ is some unknown function representing the expected response value of individuals with SNP genotype \mathbf{x}_i , i.e. the conditional expectation function $E(y|\mathbf{x}_i)$. The random vector of residuals, $\mathbf{e} = e_i$ is assumed identically and independently distributed. Here, the conditional expectation function given a vector of codes for the SNP locus p

$$g(\mathbf{x}_p) = \frac{\int \mathbf{y} p(\mathbf{x}, \mathbf{y}) d\mathbf{y}}{p(\mathbf{x})}$$

was inferred using the Nadaraya–Watson estimator (Nadaraya, 1964; Watson, 1964). The numerator and denominator in the expression above can be estimated as

$$\int \mathbf{y} p(\mathbf{x}, \mathbf{y}) d\mathbf{y} \approx \frac{1}{nh} \sum_{i=1}^n y_i K_h(x - x_i)$$

and

$$p(\mathbf{x}) \approx \frac{1}{nh} \sum_{i=1}^n K_h(x - x_i),$$

respectively, where n is the number of data points and $K_h(x - x_i)$ is a kernel function, with smoothing parameter h , which measures ‘genomic distance’ between pairs of individuals. More details on this model are in Gianola *et al.* (2006) and Gonzalez-Recio *et al.* (2008). A Gaussian kernel was used, $K(x - x_i) = \exp[-\frac{1}{2h}(x - x_i)^2]$, where $(x - x_i)$ is the genomic distance measurement. This naïve metric showed good performance in pilot studies. The genomic distance was calculated as the number of different alleles between individuals for a given SNP. The smoothing parameter h controls the decay of the function. Here, an SNP-specific h was set fixed to increase computational performance (i.e. each SNP had a possibly different h). A reasonably large value (20% of genomic distance range for each SNP, selected *ad hoc* according to the predictive ability in the testing set) was used, as suggested by Cornillon *et al.* (2008).

Appendix B

BayesA is as a Bayesian regression on SNPs assuming marker-specific variances. The model may be

expressed as

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{e},$$

where $\boldsymbol{\beta} = \{\beta_p\}$ is, e.g. the vector of 32 611 SNPs regression coefficients assumed to be distributed as $\beta_p \sim N(0, \sigma_p^2)$ ($p = 1 - 32\,611$), where σ_p^2 is the variance of the uncertainty distribution of the effect of marker p , assumed to be distributed as the scaled inverse chi-square $\sigma_p^2 \sim v_p s_p^2 \chi_{v_p}^{-1}$, with $v_p = 4$ and $s_p^2 = 0.002$ for all p . The residual variance (σ_e^2) was assumed to follow the scaled inverse chi-square prior distribution $\sigma_e^2 \sim v_e s_e^2 \chi_{v_e}^{-1}$, with $v_e = 5$ and $s_e^2 = 0.7$. \mathbf{X} was the incidence matrix relating regression coefficients on SNPs to \mathbf{y} . Details may be found in Meuwissen *et al.* (2001).

BayesA was implemented via Gibbs sampling, consisting of a single chain of 25 000 iterations, with the first 5000 iterations discarded as burn-in. The convergence of chains was inspected visually. Predicted responses in the testing set were calculated by multiplying the posterior mean of estimated coefficients by the respective SNP genotype codes of sires in the testing set, and summing over SNP loci.

Appendix C

The Bayesian counterpart of the LASSO described by Park & Casella (2008) was used to estimate the regressions on markers β_p . The original LASSO (Tibshirani, 1996) assumes the following loss function:

$$\min_{\mathbf{b}} (\mathbf{y} - \mathbf{X}\boldsymbol{\beta})'(\mathbf{y} - \mathbf{X}\boldsymbol{\beta}) + \lambda \sum_{p=1}^P |\beta_p|,$$

for some $\lambda \geq 0$, which controls the extent of shrinkage of regressions. Park & Casella (2008) suggested a fully BL with a conditional Laplace distribution placed on the regressions, that is

$$p(\beta|\sigma_e^2) = \prod_{p=1}^P \frac{\lambda}{2\sqrt{\sigma_e^2}} e^{-\lambda|\beta_p|\sqrt{\sigma_e^2}},$$

where σ_e^2 is the residual variance. Inferences about λ may be done in different ways (Park & Casella, 2008). The model was

$$\mathbf{y} = \mathbf{X}\boldsymbol{\beta} + \mathbf{e},$$

where $\boldsymbol{\beta} = \{\beta_p\}$ is the vector of 32 611 SNPs regression coefficients. Laplace priors were assigned to the SNP coefficients as stated above, and σ_e^2 was assumed to follow the scaled inverse chi-square prior distribution $\sigma_e^2 \sim v_e s_e^2 \chi_{v_e}^{-1}$, with $v_e = 5$ and $s_e^2 = 0.7$. Here, a gamma prior was assumed for λ^2 , with known rate (r) and shape (δ) hyper-parameters, as described by de los Campos *et al.* (2009). Hyper-parameters for the gamma prior distribution on λ^2 were $r = 10$ and

$\delta=0.1$. Elements of the incidence matrix \mathbf{X} -related regression coefficients for SNPs to \mathbf{y} .

The BL was implemented via Gibbs sampling, consisting of a single chain of 25 000 iterations, with the first 5000 iterations discarded as burn-in. The

convergence of chains was inspected visually. Predicted responses in the testing set were calculated by multiplying the posterior means of estimated coefficients by the respective SNP genotype codes of sires in the testing set, and summing over SNP.